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## List of Abbreviations

- **AES** All-Electric Ship
- **CPL** Constant Power Load
  - **ES** Energy Storage
- MVAC Medium Voltage Alternating Current
- **MVDC** Medium Voltage Direct Current
  - **PCM** Power Conversion Module
  - **PFN** Pulse Forming Network
  - **PGM** Power Generation Module
    - **SoC** State of Charge

## Chapter 1

### Introduction

Shipboard power systems must support higher power throughput due to the introduction of the following technologies: high power radar, electric propulsion, pulsed power loads, and high power computing [6, 12]. Some of these technologies were originally electric but with increased power consumption and capabilities. Meanwhile, other loads, such as propulsion, has shifted towards electrification for various benefits [7]. With the electrification of almost everything aboard a ship, a need arises for an all-electric ship (AES) design. However, all of these new electronics require power capabilities to support them, and ships have limited space and weight resources to support the additional hardware. The design of an AES is critical in ensuring maximum effectiveness of the ship while fitting within its tight constraints.

Shipboard medium voltage direct current (MVDC) is an ongoing effort in developing a future power system for an AES. As the name suggests, MVDC is the main power transmission format in this power system. Compared to medium voltage alternating current (MVAC), MVDC has better power density over its AC counterpart [15]. However, MVAC is a more mature technology, and more readily available for near future shipboard systems [10]. Various research and development efforts are progressing to ensure that the benefits of a future MVDC architecture can be utilized.

As with all power systems, it is important to robustly stabilize the bus voltage to ensure good power quality. In the MVDC system, the bus voltage must be capable of recovering to and maintaining a nominal voltage from large and small excitations. This is known large



#### Chapter 1. Introduction

and small signal stability. Finally, the various loads in an MVDC system will all be constant power loads (CPLs) [12]. CPLs are inherently destabilizing due to their natural voltagecurrent response behavior [14]. As voltage drops, a CPL increases current consumption, furthering the voltage drop. In a MVDC system, energy storage (ES) is critical in ensuring bus voltage stability and also maintaining load power quality and uptime [16], which is especially true when pulsed loads are present. However, ES requires space and tonnage. Therefore, it is critical in ensuring that the power and energy resources aboard the ship are fully utilized.

This thesis investigates implementing a negative load virtual small signal stabilizer for a shipboard MVDC system supporting a pulsed load. This thesis will expand the required background details in a literature review in Chapter 2, and discuss implementing a pulsed load controller in Chapter 3. Then, the stabilizer design is explained in Chapter 4 along with how to implement it. Finally, the implementation methodology is verified in Chapter 5 using simulations. From there, the stabilizer is tested with pulsed loads in Chapter 6. Discussion on the results will be handled in Chapter 7.

### **1.1** Contributions

The contributions of this thesis are the implementation of a pulsed load controller and a design for a negative load virtual small signal stabilizer for MVDC applications. A pulsed load controller is implemented and discussed, and an approach to optimizing pulse forming trigger resolution in microcontrollers is implemented. The controller was experimentally tested with a working pulsed load prototype, verifying its design.

There already exists negative load virtual small signal stabilizers for DC applications in literature. However, these methods must be adapted to MVDC applications correctly to be

#### 1.1. Contributions

effective. This thesis's design for a negative load virtual small signal stabilizer for MVDC applications advances the state of the art, because it utilizes existing shipboard MVDC reference architecture hardware from [12] instead of adding new hardware. Also, this design limits any power quality impact caused by the negative load aspect on the downstream loads. Finally, this thesis uses simulation to test the small signal stabilizer performance when pulsed loads are present.

### Chapter 2

## **Review of Literature**

### 2.1 All Electric Ship Power Systems

In traditional ship power systems, propulsion and service loads have separate dedicated power generators [6]. However, this leads to inefficient use of volume and tonnage, which are limited ship resources. Also, these loads were not necessarily active all the time, resulting in under-utilized usage of resources. An AES power system will connect together these individual power systems together using a common power distribution system. This way, each shipboard generator can be connected to any on-line load, and do not become underutilized whenever a load is unused. Integrated Power System (IPS) was the first step in advancing a centralized power distribution system [6], and shipboard MVDC is a possible next iteration.

An MVDC system has many advantages over MVAC shipboard power system designs. Firstly, the physical power bus cross section area will be more utilized [12]. Also, there is no need for synchronization hardware used in AC systems. Without the need of frequency synchronization, high frequency transformers, electric propulsion drivers, and DC/DC converters can be used. This shrinks bulky low frequency propulsion drivers and transformers in MVAC systems [15]. Higher operating frequencies provide functionality advantages to some electronics along with shrinking passive electrical components such as power filters. All of these advantages greatly increases the power density of a MVDC system over its AC

#### 2.2. Reference Shipboard MVDC Architecture

counterparts.

### 2.2 Reference Shipboard MVDC Architecture

A reference shipboard MVDC power architecture has been developed for aligning researched architectures [12]. The reference architecture is shown in Fig. 2.1. The components of this complex system can be broken down into the following components: generators, bus nodes, power converter modules (PCMs), and propulsion loads. Besides propulsion, loads will not be directly connected to the MVDC bus. Instead, PCMs will interface loads and the MVDC bus. Because PCMs have power converters as its electrical interfaces, they will behave like CPLs to the MVDC bus [19] Note that this reference architecture is not the final design of a shipboard MVDC system but rather a starting point for research, and further improvements may be made upon new developments.



Figure 2.1: General reference MVDC architecture from [12]

In the reference MVDC system, generators are put into power generation modules (PGMs). There are two different sizes of PGMs: auxiliary and primary. The auxiliary PGMs will have a lower power throughput than the larger PGMs. The purpose of this distinction

#### Chapter 2. Review of Literature

is to ensure the PGMs online are running at maximum fuel efficiency operating points. Generators operate at large time constants, meaning they will be slow in responding to fast perturbations on the MVDC bus. Also, generators cannot quickly ramp their power throughput to singlehandedly power pulsed loads.

Electric propulsion is the largest constantly running power load type in a shipboard MVDC system [22]. Propulsion power consumption can be adjusted at a slightly faster time constant than generators. The adjustment of its power consumption will affect the ship's actual movement speed, but they can be used to provide some bus voltage stabilization services. The propulsion power consumption can be temporarily shed to redirect power to a different load while the generators catch up. Also, the propulsion can also temporarily absorb excess generation whenever a load turns off. This is done by having the ship temporarily move faster than its target speed while the generators slowly reduce power throughput. Unfortunately, these propulsion systems still do not operate at fast enough time constants to fully buffer a large pulsed load [12].

The PCMs are designed to be modular and scalable in terms of what downstream loads it can support. The PCMs will have an internal DC bus and ES that is bi-directional to its internal DC bus. A set of power converters will interface the internal DC bus with the MVDC bus. Another set of power converters will feed power from the internal DC bus to downstream loads. There are two proposed variants for the PCMs: PCM-1A and PCM-1B. The PCM-1A is intended for loads up to the maximum of several single digit megawatts and to support small pulsed loads up to 1MW [9]. A generalized PCM-1A layout is shown in Fig. 2.2. The PCM-1B is intended for loads in the order of tens of MW and mainly intended to support very large pulsed loads [9].

#### 2.2. Reference Shipboard MVDC Architecture



Figure 2.2: Reference PCM-1A generalized design from [12]

#### 2.2.1 MVDC Energy Storage

Both PCM variants contain internal ES that provides hold-up power and large signal power stability services [1]. PCMs and their ES operate at very fast time constants compared to the generators and propulsion systems. This makes them ideal for providing power quality services, buffering any mismatch between generated and consumed power. Therefore, it is critical to maintain the ES is at a sufficient state of charge (SoC) to support these power quality services. Also, the ES must be sized to ensure the hold-up power is held for required MVDC reconfiguration times.

Unlike a PCM-1A, a PCM-1B can be configured to allow bi-directional power flow to the MVDC bus, providing power quality services to the entire MVDC system rather than the local load [12]. There has been work in developing a bi-directional PCM for this application [5]. However, the general layout of a bi-directional converter is putting two sets of uni-directional power converters in parallel while one set feeds power in the opposite direction of the other. This makes uni-directional solutions more desirable to save space aboard a ship.

#### Chapter 2. Review of Literature

#### 2.2.2 Fault Clearing Hold-Up Power

The hold-up power functionality is required due to the fault clearing process for the MVDC bus. DC power systems do not have a zero voltage crossing unlike AC systems. In an AC system, to isolate a fault, a physical disconnect switch is sufficient as there are points where the voltage is zero, breaking any electrical arcs. In a MVDC system, the MVDC bus must be de-energized before switching can occur.

To clear a MVDC bus fault, switching is done to isolate the faulty bus segment. After the fault is isolated, more switching is done on the MVDC bus to reconfigure its power distribution routing. Therefore, all loads will lose power from the MVDC bus and must rely on their local ES during this entire process [21]. Since some of these critical loads can consume large amounts of power, the ES capacity can be fairly large. Also, the ES must maintain a fairly high SoC to ensure that hold-up energy is always available for when a fault occurs.

Depending on the MVDC bus fault protection topology used, protective devices such as a solid state DC breaker must be added to all MVDC bus power sources [8], consuming additional space and tonnage resources. Bi-directional PCM-1Bs or ES directly attached to the MVDC bus are considered power sources. Therefore, there can be even more space and tonnage savings for implementing PCM ES in a uni-directional configuration.

### 2.2.3 Large Signal Stabilization

Large signal stability generally refers to a how well a system can compensate or recover from a very large perturbation that causes great deviations from designed operating points. CPLs make the MVDC system non-linear, but for small signal stability, the stability criteria is often linearized along set operating points [2]. However, such a criteria does not apply when

#### 2.2. Reference Shipboard MVDC Architecture

large disturbances bring the system outside those operating points. Large signal stability is required to handle the non-linear behavior of the system.

An example of a large signal perturbation would be loads that have wide power consumption swings, such as pulsed loads. Power pulsing can cause drastic voltage sagging, and the peak pulsed load power consumption can quickly exceed on-line generation. The peak power and ramp rate of large pulsed loads can easily out pace generators. The ES is critical in compensating for the slow generators and limit drastic system operating point changes [22].

To prevent pulsed loads from transmitting its large destabilizing effect onto the MVDC bus, the local PCM ES is used for large signal stabilization. The ES balances the large mismatch between available generation and power consumption of the pulsed load [25]. The PCM slowly ramps its power consumption from the MVDC bus in a stable manner while the ES supplies or absorbs the missing or excess power of the pulse. This way, the generators will only see a slow ramping load on the MVDC bus. The ES will slowly discharge of recharge later on to normalize its SoC.

#### 2.2.4 Small Signal Stabilization

Small signal stability describes whether a system maintains a stable state by its inherent responses when disturbed by a small, continuous disturbance. Such disturbances within a shipboard MVDC system can come from various sources such as:

- Generator output impedance and ripple voltage
- Bus resistance, inductance, and/or capacitance interactions
- Constant power loads responding to bus voltage fluctuations
- System controllers making slight adjustments

#### Chapter 2. Review of Literature

In power systems, small signal stability is provided by damping the system responses to converge towards a set value. This can be done by adding passive components such as inductors and capacitors, or by tuning control variables. In a shipboard power system, it is ideal that small signal stability requires the minimal amount of added hardware to save space and weight. Also, if the MVDC system reconfigures its power distribution routing due to a fault, the new configuration may change the MVDC bus's electrical characteristics and small signal stability. A tunable control variable is easier to adjust than changing the stabilizing hardware.

### 2.3 Negative Load Virtual Stabilization

It is possible to emulate stabilizing circuit hardware by implementing the behavior in a control loop. This is called a virtual stabilizer. An example would be a DC/DC converter sourcing or draining current mimicking a capacitor model. From there, instead of changing a real capacitor's capacitance, the converter's controller will only need to change a control variable to change its effective capacitance. A virtual stabilizer can be implemented in the PCMs of a MVDC system.

As mentioned before, having PCMs capable of bi-directional power flow to the MVDC bus will require additional hardware, which is undesirable. A virtual stabilizer can function off uni-directional PCMs by using a negative load configuration. In a negative load stabilizer, a load's consumed power is reduced or increased as if the stabilizer is in parallel with the load. However, negative load stabilizers are limited by the power consumed by the real load and can never operate without the real load consuming power. There are examples of negative load virtual stabilizers in literature outside of shipboard MVDC applications.

[26] works with a 48V DC circuit with RLC parasitics in front of a uni-directional DC/DC

#### 2.3. Negative Load Virtual Stabilization

converter. [26] implemented various virtual negative load stabilizer configurations such as parallel RC, parallel RL, series RL, and parallel RLC. The paper deemed that the impact of the virtual stabilizer on the down stream CPL was negligible.

[17] added a virtual parallel capacitor as a stabilizer to satisfy  $P < \frac{RCV^2}{L}$  to dampen the DC bus RLC parasitics with a CPL motor, guaranteeing small signal stability. Despite the paper not stating this, it should be noted that the control loop used in this paper actually uses a virtual parallel RC stabilizer. The virtual R component was introduced in the control loop's low-pass filter. No where in this paper was the virtual resistor mentioned, but analysis was done including the component. This paper assumed the motor controls were efficient enough to not be affected by the stabilizer's power fluctuations.

Though a shipboard MVDC system has higher power and voltage levels than these papers, there are many advantages that a shipboard MVDC can have with negative load virtual stabilizers. The system can be fine tuned by software after any MVDC bus reconfiguration, and the PCM has internal ES that can cancel any power fluctuations on the load. With such a stabilizer implemented in existing hardware, there can be space and weight savings, too.



## Chapter 3

## **Pulsed Power Loads**

A diagram of an example shipboard MVDC power system with pulsed loads is shown in Fig. 3.1. The components of a typical pulsed power load is shown in the large pulsed power load block of the figure.



Figure 3.1: Example Layout of a MVDC System with Pulsed Loads

A typical pulsed power load contains a pulse forming network (PFN) to supply the end load's power pulse. This is because a pulsed load often require a fast peak power than cannot be supplied by traditional power systems. A PFN generally consists of: its own fast discharge ES, a charger to charge the PFN ES, and an output power pulser that generates the desired pulse shape. A PFN's ES will slowly charge up before suddenly releasing it to drive the load.

In shipboard MVDC, the shipboard MVDC system will only see the charging of the pulsed load's PFN ES [23]. Therefore, the MVDC system will never see the actual power pulse at the end load within the pulsed load. However, the charging power curve of a PFN can be very aggressive, where the pulsed load charging itself is a power pulse. This is because pulsed loads may need to operate multiple times a minute, requiring a train of power pulses to recharge it [22]. Recharging the all of the ES must be done quickly enough to maintain its desired rate of use.

With the entire MVDC system, the fast PCM ES will be used to buffer the large transient power consumption of the pulsed load charging its PFNs. The faster PFN ES within the pulsed load buffers the even larger and shorter power pulse for the end load. Basically, the same energy from the generator is having its power delivery time shortened and peak power increased at each successive ES device.

To better understand the functionality of a pulsed load, a controls system was implemented and experimentally tested for a prototype pulsed load. The pulsed load prototype employs capacitor-based PFN ES, and uses thyristor-based switching for pulse forming. A circuit of the pulsed load is shown in Fig. 3.2

In this pulsed load prototype, the PFN ES is divided into separate capacitor banks, where the controls system will selectively charge them using relays. The charger itself can be controlled to charge the desired amount of energy. The gate drivers are triggered by the

Chapter 3. Pulsed Power Loads



Figure 3.2: Pulsed Load Prototype Circuit Diagram

controls system to drive the thyristors switch, sending current from the PFN ES through and inductor and into the load.

The controls system implementation and experimental results are available in Section 3.1. Minus some scaling difference, the components of the pulsed load prototype are similar to a typical pulsed load in a shipboard MVDC system. With a good understanding of pulsed loads, it is necessary to tackle the MVDC stability problems that pulsed load charging introduces.

## 3.1 Implementing a Controller for a Pulsed Load Prototype

A controls system for a pulsed load was implemented and experimentally tested. A block diagram of the pulsed load system is shown in Fig. 3.3.





Figure 3.3: Implemented Pulsed Load Hardware Block Diagram

The majority of the pulsed load is the pulse forming network (PFN). The PFN consists of PFN modules, PFN charger, and controllers. The PFN modules are composed of: a capacitor bank for ES, semiconductor switch, and output pulse forming circuitry. The PFN charger is the charging power supply unit (PSU) in the block diagram.

The controls system has a user interface at the controls computer implemented using Lab-VIEW. The controls computer will remotely send commands to the charging and pulsing controllers, and it will receive system data from the multiplexed data acquisition (DAQ) hardware. The charging controller controls how much energy to store in the PFN along with other auxiliary hardware. The pulsing controller discharges the PFN modules into the load in a controlled manner for the desired power pulse waveform. If this system were to be installed in a shipboard MVDC system, the entire PFN and load would be considered the pulsed load. The PFN charging power would be the power pulse seen by the MVDC system. In Fig. 3.3, the dedicated power line would represent the MVDC PCM power source to its downstream loads.

### 3.1.1 Pulsed Load Control Overview

The implemented controls system is operated by a state machine implemented in LabVIEW. The states are shown below in Fig. 3.4. The states basically correspond to the steps needed to operate a typical pulsed load.

First, the system operator boots up the controls system from an idle state. The operator configures the PFN along with running any auxiliary setup required by the pulsed load. The control system then charges the PFN modules to the specifications of its configuration, and disconnects the PFN charging power supply after charging is complete. From there, the pulse timings are sent to the PFN, and the PFN outputs the power pulse to the pulsed load. After pulsing is completed, the PFN safes itself from any residual energy. The software gathers any collected data from various sensors in the system and stores it for later analysis. Afterwards, the controls system shuts down the PFN, awaiting the operator to boot it up for another pulse.

The implemented controls system software is sophisticated in that it automates many processes such as charging, preventing operator error. Error detection and automatic pulse aborting is implemented to protect the hardware from damage when an anomaly is detected. Due to the high energy nature of pulsed loads, the system was design to fail into a safe state with whatever surviving hardware remains after a fault.

#### 3.1. Implementing a Controller for a Pulsed Load Prototype



Figure 3.4: Implemented PFN Controls System State Diagram

### 3.1.2 Pulsing Controller Optimization

Optimization of the pulsing controller firmware was implemented to improve PFN discharge timing resolution from microsecond units to nanosecond units. A fine resolution for the PFN discharge timings is critical to accurately generate the desired output pulse shape.

The original discharge timing code was implemented in C. The code would receive the discharge timings and use conditional checks and loops to discharge each PFN module at the desired times. However, it takes precious clock cycles to check each condition and handle looping logic, limiting the discharge timing resolution.

To optimize this code, a machine code assembler was implemented using C. When the pulsing controller receives the PFN module discharge times, it writes machine code with the precise CPU instructions sequence to discharge the PFN modules at the correct times. This machine code was written in a reserved partition of the microcontroller's RAM. Many sets of "no

Chapter 3. Pulsed Power Loads

operation," or NOP, CPU instructions were used to idle the microcontroller until the CPU program counter reaches instructions to send a PFN module discharge signal. Therefore, all of the condition checking and loop logic were replaced by the precise wait time needed by the discharge timings. For long wait times between discharge signals, a loop of NOPs is generated, and filler NOPs are added to the exact needed wait time. The general logic of this assembler is shown in Algorithm 1.

Alg	Algorithm 1 Pulsing Machine Code Assembler		
1:	if Receive PFN Module Pulse Timings then		
2:	Write: Initialize CPU Registers For Pulsing		
3:	for all Pulse Times do		
4:	if Long Delay then		
5:	Write: Looping Long Delay		
6:	for all Left Over Delay Times do		
7:	Write: Filler NOP Delays		
8:	Write: Send Discharge Signal		
9:	else if Short Delay then		
10:	for all Delay Times do		
11:	Write: NOP Delays		
12:	Write: Send Discharge Signal		
13:	else		
14:	Write: Send Discharge Signal		
15:	Write: Jump to Jump Return Register Address		
16:	Store Current Data of CPU Registers		
17:	Jump and Store Return to Machine Code RAM Partition Start Address		
18:	Restore Data of CPU Registers		

Before any pulse timings are assembled, the assembler writes machine code to pre-load the CPU registers. This is to prevent the need of loading data into the registers during the timing critical portions of the machine code. The assembler tracks discharge delay times and the current write memory address to write to. It ensures that the long delay loops and NOPs are written in such a way to minimize memory usage, because the reserved RAM partition is limited in size. The write to memory address is simply constantly incremented each time a CPU instruction is entered by the assembler.

18

#### 3.1. Implementing a Controller for a Pulsed Load Prototype

Once the discharge timings are assembled, the current data in the CPU registers are stored, because the C code compiler does not expect and handle the injected machine code modifying CPU register values. The C code jumps to the assembled machine code, pre-loads the registers, and runs the discharge timing code. Afterwards, the machine code returns to where the C code left off, and the C code restores the CPU registers before continuing on as normal as if nothing happened.

This optimization is hardware specific to PIC32 microcontrollers, which was used in this implementation. A weakness of an assembler optimization solution is that it is not portable to other microarchitectures. Ideally, for parallel timing operations, a FPGA would be used here. However, the pulsing controller has a lot of other logic that would require a microcontroller to easily implement, and the optimized implementation produces more than adequate results for this system.

### 3.1.3 Pulsed Power Load Experimental Results

The implemented controls system was used to experimentally test the complete pulsed load system. Various experiments were done with successful results, confirming the functionality of the controls system. An example output power pulse from the PFN is shown in Fig. 3.5.

The ideal output of the PFN is a square pulse at a set amount of peak power for a set amount of time, so the goal is to have the implemented PFN achieve a square pulse as closely as possible. However, with real hardware, there are rise and fall times for the PFN. Also, the peak current of the square pulse is not flat due to the output current waveforms of a single PFN module. Instead, controlled PFN module discharging at the correct times are used to generate an as flat as possible peak current, which is made possible by the optimized pulsing controller. Thanks to the optimized resolution of the pulsing controller, pulse timing errors

Chapter 3. Pulsed Power Loads



Figure 3.5: PFN Output Power Pulse to Pulsed Load

were not discernible or non-existent.

## Chapter 4

# Proposed MVDC Small Signal Stabilizer

This thesis designs a negative load virtual small signal stabilizer in a uni-directional PCM for a shipboard MVDC system to support pulsed loads. The ES will be used to cancel out the stabilizer's power fluctuations on the downstream load. This stabilizer should guarantee small signal stability across a wide power range seen in pulsed loads. Because pulsed loads will greatly change its equivalent load resistance on the MVDC bus, this thesis proposes to dynamically tune the virtual stabilizer with the load power consumption.

To implement the stabilizer, a working MVDC model needs to be developed. Also, control loops must be made for the various functions of the PCM. From there, a small signal stability criteria needs to be developed. Finally, method of tuning the stabilizer to be stable is needed.

### 4.1 Simplified MVDC Model

As mentioned before, the reference MVDC model is fairly complex. For the sake of developing and testing a this negative load stabilizer design, the MVDC system model has been simplified into what is shown in Fig. 4.1. This model has a single ideal generator with voltage droop. There is a generic reference design PCM which has an internal DC bus with a bus capacitor, internal ES, and the downstream constant power load. Each of the DC/DC



#### Chapter 4. Proposed MVDC Small Signal Stabilizer

power converters within the PCM have power and power ramp rate limitations and follow the power flow of a reference PCM-1A.



Figure 4.1: Simplified MVDC model used for testing.

The is a RLC component that is a simplified representation of the electrical characteristics of a generator, power converter with filter, and MVDC bus as discussed in Section 2.2.4. This was done assuming that the system could be represented as such done in [12]. This model can be converted to a more complex model by: separating out the electrical characteristics, expanding the power converter with input filter values and switching, and/or add a parallel PCM on the MVDC bus.

Without the virtual stabilizer in the simplified circuit, the small signal stability criteria is

$$P < \frac{RCV_{MVDC}^2}{L},\tag{4.1}$$

where P is the power consumption of the PCM from the MVDC bus,  $V_{MVDC}$  is the MVDC bus voltage at the PCM, and R, L, and C are the RLC characteristics of the MVDC bus. Note that  $V_{MVDC}$  may fluctuate due to noise or voltage droop, and P will also change drastically during power pulsing. Therefore, the above small signal stability criteria must

#### 4.2. Control Loops

considered for all operating points.

### 4.2 Control Loops

A set of control loops were developed to control the PCM's internal behavior and interactions with the MVDC bus. The controller maintains the internal bus voltage while allowing the virtual stabilizer to inject power on its MVDC input power converter. Also, the controller manages and utilizes the ES while ensuring power quality to the downstream constant power load. The ES control loop uses the ES for internal bus regulation while the MVDC side power converter control loop attempts to balance power consumption with power sourced from the MVDC bus.

A number of the following control loops used in this thesis were adapted from other papers. Besides the virtual stabilizer control loop, the PCM control loops were adapted from [6]. These control loops were intended for a zonal DC bus with a generator, ES, PCM power input from an MVDC bus, and CPL. These control loops were not tested with pulsed power loads.

The MVDC bus to PCM internal DC bus DC/DC power converter control loop adapted from [6] is shown in Fig. 4.2. The control loop's  $i_{G0}$  has been removed as there is no generator inside the reference PCM design. Also, the controls delay transfer functions have been removed to simplify the model.



Figure 4.2: MVDC Side Power Converter Control Loop from [6]

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The modified MVDC side power converter controls loop used in this thesis is shown in Fig. 4.3.  $i_L$  is the CPL's current at the internal bus voltage  $V_{IBus}$ .  $\bar{i}_{ES}$  is the set ES recharge current at  $V_{IBus}$ .  $i_{C_V}$  is the current of the virtual stabilizing capacitor at  $V_{IBus}$ .  $\frac{d}{dt}i'_{PGM}$  is a virtual ramp rate limit on the MVDC side power converter. This represents the equivalent MVDC bus generator's power ramp rate limitations as a current at  $V_{IBus}$ , and loads should not exceed the generator's ramp rate limits.  $i_{PCM}$  and  $\frac{d}{dt}i_{PCM}$  are the actual current and ramp rate limits of the MVDC side power converter at  $V_{IBus}$ . The extra ramp rate was applied because the virtual capacitor is not a "real" load, and does not obey the generator limits to provide stabilization services. However, the PCM is implementing the virtual stabilizer and must obey its own limitations.



Figure 4.3: Modified MVDC Side Power Converter Control Loop

For the virtual capacitor stabilizer, the power of the virtual capacitor is

$$P_{C_V} = C_V V_{MVDC} \frac{dV_{MVDC}}{dt}.$$
(4.2)

The virtual capacitor stabilizer control loop was adapted from [17], and it is recreated below in Fig. 4.4. There is low-pass filter in this control loop that was implemented by subtracting the output of a high-pass filter from the original signal. [17] did not explicitly state that there was an added virtual resistance, but there is one due to the nature of the low pass

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filter in the control loop.



Figure 4.4: Original Virtual Capacitor Stabilizer from [17]

This thesis converted the control loop's virtual capacitor's power  $P_{VC}$  to the virtual capacitor's, or stabilizer's, current  $i_{VC}$  at  $V_{IBus}$ . Hardware limits were also incorporated on the virtual capacitor. These limits were applied because the converter hardware cannot completely replicate a real RC stabilizer behavior, and the control loop should reflect this. Also, the low-pass filter configuration was simplified in this thesis's control loop into a transfer function based on the virtual resistor  $R_V$  and capacitor  $C_V$  values.



Figure 4.5: Modified MVDC Side Power Converter Control Loop

PCM hardware limits were applied to the virutal capacitor, because the PCM is emulating the "real" equivalent hardware. As stated before, the ramp rate limit  $\frac{d}{dt}i'_{PGM}$  is a virtual limit to follow an MVDC bus generator's ramp rate limits. The virtual stabilizer is not

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a "real" load, and it must function as closely to a real stabilizer to provide stabilization. Therefore, the generator's ramp rates were ignored and the PCM's ramp rate limits were used instead. Furthermore, the PCM's power limits were applied in plus-minus form as the stabilizer can only change PCM power to zero at full PCM power or to full power at no PCM power. Later on in the PCM's control block, the  $i_{C_V}$  term will be added up and have the PCM's ramp rate and power limitations re-applied to ensure all of the PCM's limitations are obeyed.

The ES control loop has been modified from [6], with the original control loop replicated in Fig. 4.6. [6] used a simple proportional controller for internal bus voltage regulation. The ES that was used had infinite energy, and the injected  $i_{E0}$  is to manually set the current contributed by the ES. Finally, a control delay transfer function as added at the end. V is the current bus voltage and  $V^*$  is the nominal bus voltage.



Figure 4.6: ES Control Loop from [6]

This thesis removes the controls delay and adds current ramp rate and saturation limits. Because the ES must be at or near its nominal energy level whenever possible to provide hold-up power at any time, this thesis assigns finite energy capacity to the ES. The modified ES bus voltage regulation control loop is shown in Fig. 4.7 with an additional ES control loop to return to nominal SoC shown in Fig. 4.8.

The original V and V<sup>\*</sup> have been replaced with  $V_{IBus}$  and  $V_{IBus}^*$  to represent that the regulated bus voltage is specifically the PCM's internal DC bus.  $\bar{i}_{ES}$  represents the ES

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Figure 4.7: Modified ES Bus Voltage Regulation Control Loop

nominal energy regulator control loop output from Fig. 4.8.  $i_{C_V}$  represents the current of the virtual capacitor stabilizer at  $V_{IBus}$  as the ES will need to cancel out the power fluctuations of the virtual stabilizer to maintain power quality. Finally,  $\frac{d}{dt}i_{ES}$  and  $i_{ES}$  ramp rate and saturation limits were applied to represent the physical power limitations of the ES hardware.

The proportional controller was replaced with a proportional-integral controller. The integral term is required for pulsed loads. This is because the internal DC bus voltage will sag from aggressive load power consumption ramp rates. With only the proportional term, the voltage sag will only grow worse as the CPL current will increase upon voltage sag, overpowering the error correction of the proportional only controller. If the proportional controller's coefficient  $K_P$  is very high to compensate for voltage sag, the internal DC bus voltage will become unstable.  $V_{IBUS}$  will oscillate and grow away from  $V_{IBUS}^*$  and never converge. The integral term corrects the voltage sag over time with even more current, preventing the increased CPL current from collapsing the bus voltage. The integral term removes the need of a high  $K_P$ , preventing the proportional term from becoming unstable.

Since the ES is finite, an ES energy management control loop was developed and shown in Fig. 4.8

 $E_{ES}$  is the current ES energy.  $E_{ES}^*$  is the nominal energy that the ES should normally stay at.



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Figure 4.8: ES Energy Regulator Control Loop

The ES should not destabilize the DC buses and obey the generator limits when recharging or discharging to nominal  $E_{ES}^*$ , so the ES energy regulation is limited by the MVDC generator's ramp rate limits and PCM's current limits. The ES will also never attempt to return to nominal energy levels when the internal bus voltage  $V_{IBus}$  is not within its tolerances Tol as the ES's first role is to regulate the internal DC bus voltage. A proportional controller was used to return the ES to its nominal SoC, allowing a more aggressive charge/discharge the further  $E_{ES}$  is from  $E_{ES}^*$ .

The proportional controller's coefficient  $K_R$  must be large enough so that the ES will return to nominal SoC fast enough, but it cannot be too large where the SoC  $E_{ES}$  will not stably converge towards  $E_{ES}^*$ . The  $K_R$  term must follow the criteria  $K_R < \frac{1}{V_{IBUS}}$ . This is because  $E_{ES}^*$  and  $E_{ES}$  are in units of Joules of energy, and the output of this control loop  $i_{ES}$  is in units of current at  $V_{IBUS}$ . With  $K_R = 1$ ,  $V_{IBUS}$  of power will be used to charge/discharge 1J of energy difference between  $E_{ES}$  and  $E_{ES}^*$ . If  $V_{IBUS} > 1$ ,  $E_{ES}$  would overshoot and never converge to  $E_{ES}^*$  as >1W is used to charge/discharge the 1J error. Since  $V_{IBUS}$  may fluctuate, a safety margin on  $K_R$  is required.
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### 4.2.1 Voltage Droop

Voltage droop is useful for current sharing of parallel generators or power converters [11]. Therefore, it is important to allow the MVDC bus voltage to quickly settle. To allow this, the stabilizer must avoid overly over-damping the system, which can be a dynamic tuning criteria.

The voltage droop used in this model is defined as

$$V_{Droop} = V_{NL} - \left(\frac{i_{PGM}}{i_{PGMMax}}\right) \left(V_{NL} - V_{FL}\right),\tag{4.3}$$

where  $V_{NL}$  is the voltage droop at no load on the generators,  $V_{FL}$  is the voltage droop at full load on the generators,  $i_{PGM}$  is the current generator output current, and  $i_{PGMMax}$  is the max output current of the generator. The  $\frac{i_{PGM}}{i_{PGMMax}}$  ratio of all generators in the system should be equal when the generators are balanced via voltage droop.

### 4.2.2 Controls Bandwidth

Controls bandwidth is important to keep in mind to ensure that this proposed small signal virtual stabilizer is realistically feasible. The controller cannot actuate a real power converter faster than the power converter's switching speed. At maximum, the controller has a maximum operating frequency of half the converter's switching frequency. Ideally, the controller should operate at most  $\frac{1}{4}$  the converter's switching frequency.

The virtual  $C_V$  and  $R_V$  should result in an operating bandwidth of no more than  $\frac{1}{4}$  of the converter's switching frequency, too. This is so that the converter is capable of generating a power waveform mimicking a real RC stabilizer's waveform. Silicon carbide power converters

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for MVDC applications are being developed, and they have higher switching frequencies than their traditional silicon-only power electronics [4]. With silicon carbide power converters, the switching frequency can be in the range of tens of kHz for MVDC applications [20].

### 4.2.3 Equivalent Circuit

The simplified MVDC system shown in Fig. 4.1 can be simplified into a system of equivalent passive components. The equivalent circuit is shown in 4.9.



Figure 4.9: Simplified MVDC model used for testing.

The  $R_V$  and  $C_V$  represents the virtual stabilizer implemented in the PCM's controls. The  $R_L$  is the equivalent resistance of the PCM as a CPL at a set voltage and power draw. Though the PCM has internal ES, if the downstream CPL of the PCM is not ramped faster than the generator's ramp rate limits of  $\frac{d}{dt}i'_{PGM}$ , then the  $R_L$  will accurately represent the downstream CPL itself as the PCM ES will not compensate for any generator power mismatch.

#### 4.2. Control Loops

### 4.2.4 Transfer Function

Using the equivalent circuit representation of the MVDC system, a  $3^{rd}$  order transfer function can be derived. CPLs act and can be modeled as a negative resistor [14]. Therefore, for accurate modeling,  $R_L$  is negative when calculating the transfer function. The transfer function of the equivalent circuit is

$$\frac{V_L}{V_D roop} = \frac{b_1 s + b_0}{a_3 s^3 + a_2 s^2 + a_1 s + a_0},\tag{4.4}$$

where

$$b_{1} = C_{V}R_{V}R_{L}$$

$$b_{0} = R_{L}$$

$$a_{3} = CC_{V}LR_{L}R_{V}$$

$$a_{2} = CLR_{L} + C_{V}LR_{L} - C_{V}LR_{V} + CC_{V}RR_{L}R_{V}$$

$$a_{1} = CRR_{L} - L + C_{V}RR_{L} - C_{V}RR_{V} + C_{V}R_{L}R_{V}$$

$$a_{0} = R_{L} - R.$$

$$(4.5)$$

It is difficult to solve this transfer function analytically. To solve for  $C_V$  and  $R_V$  to maintain a desired MVDC damping factor  $\zeta$ , low-Q approximation was used.



# 4.3 Low-Q Approximation

Low-Q approximation allows order reduction of polynomials into their approximate  $1^{st}$  and  $2^{nd}$  order roots. In the equivalent circuit's use case, the polynomial is the transfer function's poles (denominator). This makes it possible to reasonably approximate the roots of high order transfer functions. However, the roots must be real and well separated for low-Q approximation to be accurate [18]. The further the roots are separated results in a more accurate approximation. [18] shows the original mathematical proof for  $2^{nd}$  order polynomials, and [13] has expanded low-Q approximation to a more general case to support higher than  $2^{nd}$  order polynomials.

[13] has also defined special cases where only two roots are close together. The close together roots can remain in quadratic form while the other roots are in  $1^{st}$  order form. Only quadratic roots were covered by [13], but it is theoretically possible to keep roots in higher order (e.g. cubic) forms if more than 2 roots are close together. This section will only provide the low-Q approximation methodology and formulation for the transfer function Eq. (4.4) for the model in Fig. 4.9, but more information can be found about the general low-Q approximation methodology in [13].

First, the inequalities used in low-Q approximation are defined using significant inequalities  $(\gg \text{ and } \ll)$ . Let the term  $\alpha$  represent how significant the inequality is. Therefore, if  $a \gg b$ , then  $a\alpha > b$ . This value is important for low-Q approximation as a smaller  $\alpha$  means that the roots are further separated and results in a more accurate approximation [18]. With a more accurate approximation, the correctness of the stabilizer is greater, so it is important to record how accurate the low-Q approximation was done.

Next, the transfer function D(s) must be converted into the standard low-Q approximation form of

#### 4.3. Low-Q Approximation

$$D(s) = 1 + a_1 s + a_2 s^2 + a_3 s^3.$$
(4.6)

To put the original transfer function Eq. (4.5) into standard form Eq. (4.6), simply divide  $a_1, a_2, a_3$  by  $a_0$  in Eq. (4.5). This results in the standard form roots of:

$$\hat{a}_{3} = \frac{a_{3}}{a_{0}}$$

$$\hat{a}_{2} = \frac{a_{2}}{a_{0}}$$

$$\hat{a}_{1} = \frac{a_{1}}{a_{0}}$$

$$\hat{a}_{0} = \frac{a_{0}}{a_{0}} = 1.$$
(4.7)

From Eq. (4.7), the D(s) in standard form is now:

$$D(s) = 1 + \hat{a}_1 s + \hat{a}_2 s^2 + \hat{a}_3 s^3.$$
(4.8)

In low-Q approximation, if all the roots are real and well separated, the roots can be separated into only  $1^{st}$  order roots. Since Eq. (4.4) is a  $3^{rd}$  order transfer function and if all the conditions are satisfied, there will only be three  $1^{st}$  order roots. Being  $3^{rd}$  order, there are also two special cases for the low-Q approximation of Eq. (4.4). These special cases result in one  $1^{st}$  order root and one  $2^{nd}$  order (quadratic) root.

The 2<sup>nd</sup> order roots from low-Q approximation are in the form of

$$1 + \frac{s}{Q\omega_0} + \left(\frac{s}{\omega_0}\right)^2. \tag{4.9}$$

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Using Eq. (4.9), the natural frequency  $\omega_0$  can be extracted from the  $s^2$  coefficient. Then, the Q factor Q can be solved for from the s coefficient. With the Q factor, the approximate damping factor  $\zeta$  of the circuit can be solved with

$$\zeta = \frac{1}{2Q}.\tag{4.10}$$

Finally, low-Q approximation for the circuit in Fig. 4.9 can be done in the following steps. First, the normal low-Q approximation case's conditions are checked.

For the normal case, if

$$\left|\hat{a}_{1}\right| \gg \left|\frac{\hat{a}_{2}}{\hat{a}_{1}}\right| \gg \left|\frac{\hat{a}_{3}}{\hat{a}_{2}}\right|,\tag{4.11}$$

then the roots of the denominator are

$$D(s) \approx (1 + \hat{a}_1 s) \left( 1 + \frac{\hat{a}_2}{\hat{a}_1} s \right) \left( 1 + \frac{\hat{a}_3}{\hat{a}_2} s \right).$$
 (4.12)

Due to the 1<sup>st</sup> order roots, no natural frequency of the circuit can be low-Q approximated, resulting in no resonating circuit to dampen. The roots in Eq. (4.12) are shown in an order such that each successive root has a smaller time constant magnitude, which may be desirable to know for characterizing the circuit behavior. However, the normal case is only possible with certain values. Because it is desirable to shrink the real capacitor capacitance C as much as possible, C will approach L. This will result in the normal case being violated and often involve invoking the special low-Q approximation cases.

### 4.3. Low-Q Approximation

# 4.3.1 Low-Q 1<sup>st</sup> Special Case

If the normal case condition Eq. (4.11) is violated by

$$\left|\hat{a}_{1}\right| \gg \left|\frac{\hat{a}_{2}}{\hat{a}_{1}}\right| \gg \left|\frac{\hat{a}_{3}}{\hat{a}_{2}}\right|,\tag{4.13}$$

but satisfies the inequality

$$\left. \frac{\hat{a}_2^2}{\hat{a}_3} \right| \gg \left| \hat{a}_1 \right| \gg \left| \frac{\hat{a}_3}{\hat{a}_2} \right|,\tag{4.14}$$

then the  $1^{st}$  special case roots are

$$D(s) \approx \left(1 + \hat{a}_1 s + \hat{a}_2 s^2\right) \left(1 + \frac{\hat{a}_3}{\hat{a}_2} s\right).$$
 (4.15)

The  $1^{st}$  special case  $2^{nd}$  order root has an approximate natural frequency of

$$\omega_{0_1} = \sqrt{\frac{1}{\hat{a}_2}},\tag{4.16}$$

an approximate Q factor of

$$Q_1 = \frac{\frac{1}{\hat{a}_1}}{\omega_{0_1}},\tag{4.17}$$

and an approximate damping factor of

$$\zeta_1 = \frac{1}{2Q_1}.$$
(4.18)

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Note that there are subscripts indicating that these approximate values were generated from the 1<sup>st</sup> special case. This distinction is important, because when picking the stabilizer's  $C_V$ and  $R_V$  values, there are two possible value sets as the stabilizer's values chose will affect which special case that the circuit will fall under.

# 4.3.2 Low-Q 2<sup>nd</sup> Special Case

If the violation of condition Eq. (4.11) is

$$\left|\hat{a}_{1}\right| \gg \left|\frac{\hat{a}_{2}}{\hat{a}_{1}}\right| \gg \left|\frac{\hat{a}_{3}}{\hat{a}_{2}}\right|,\tag{4.19}$$

and satisfies

$$\left|\hat{a}_{1}\right| \gg \left|\frac{\hat{a}_{2}}{\hat{a}_{1}}\right| \gg \left|\frac{\hat{a}_{0}\hat{a}_{3}}{\hat{a}_{1}^{2}}\right|,\tag{4.20}$$

then the  $2^{nd}$  special case roots are

$$D(s) \approx (1 + \hat{a}_1 s) \left( 1 + \frac{\hat{a}_2}{\hat{a}_1} s^2 + \frac{\hat{a}_3}{\hat{a}_1} s^2 \right).$$
(4.21)

The  $2^{nd}$  special case  $2^{nd}$  order root has an approximate natural frequency of

$$\omega_{0_2} = \sqrt{\frac{1}{\left(\frac{\hat{a}_3}{\hat{a}_1}\right)}},\tag{4.22}$$

an approximate Q factor of

#### 4.3. Low-Q Approximation

$$Q_2 = \frac{\frac{1}{\left(\frac{\hat{a}_2}{\hat{a}_1}\right)}}{\omega_{0_2}},\tag{4.23}$$

and an approximate damping factor of

$$\zeta_2 = \frac{1}{2Q_2}.$$
 (4.24)

It may be desirable to use virtual stabilizer values that cause the system to fall into a 2<sup>nd</sup> special case low-Q approximation solution. This is due to how the successive roots in low-Q approximation have a smaller time constant magnitude [13]. Using the 2<sup>nd</sup> case results in the smaller time constant term becoming more dominant in the system's response, causing a faster response. Since the purpose of this stabilizer is to provide small signal stability, a faster response by the system is desirable, and the earlier and slower root terms can be compensated by a faster compensator. However, targeting for a solution in the 1<sup>st</sup> case can also be desirable as the 1<sup>st</sup> case's solution often has a smaller  $C_V$  value.

### 4.3.3 Low-Q Solution Space

To visualize the low-Q approximation solution space, the following algorithm was used to plot the damping factor in a space of  $C_V$  and  $R_V$ . The algorithm is a basic brute force algorithm that numerically solves for each  $C_V$  and  $R_V$  value of the virtual stabilizer to find the resulting system damping factor.

An example plot is shown in Fig. 4.10. There are two visible solution regions, and each region corresponds to a special case. The special case solution regions generally sandwich a forbidden region in between before merging at a high  $C_V$  value. The forbidden region is caused by the approximation falling outside of the normal and special cases, where the

Algorithm 2 Low-Q Approximation Brute-Force Damping Factor of Virtual RC Stabilizer

1: Initialize  $R, L, C, R_L$ 2:  $C_V Set \leftarrow$  Set of  $C_V$  searched 3:  $R_V Set \leftarrow$  Set of  $R_V$  searched 4:  $\zeta \leftarrow \text{Zero matrix of dimension } [C_V Set, R_V Set]$ 5:  $\alpha \leftarrow \text{Desired Low-Q}$  Approximation Accuracy 6: for all  $C_V$  in  $C_V Set$  do for all  $R_V$  in  $R_V Set$  do 7:  $a_3, a_2, a_1, a_0 \leftarrow \text{Calculate Transfer Function}(R, L, C, R_L, C_V, R_V)$ 8:  $\hat{a}_3, \hat{a}_2, \hat{a}_1 \leftarrow \text{Normalize}(a_3, a_2, a_1, a_0)$ 9: Calculate Case $(\hat{a}_3, \hat{a}_2, \hat{a}_1)$ 10:if Normal Case then 11:  $\zeta[C_V, R_V] \leftarrow$  No Damping Factor 12:else if 1<sup>st</sup> Special Case then 13: $\zeta[C_V, R_V] \leftarrow 1^{st}$  Special Case Damping Factor 14: else if  $2^{nd}$  Special Case then 15: $\zeta[C_V, R_V] \leftarrow 2^{nd}$  Special Case Damping Factor 16:else 17: $\zeta[C_V, R_V] \leftarrow \text{Invalid}$ 18:19: Plot  $\zeta$ 

roots are not well separated. Roots that are not well separated results in less accurate low-Q approximations. As the root separation tolerance  $\alpha$  tightens, the forbidden region will grow outward as closer roots will not be allowed.

It is visible that the solution in the 1<sup>st</sup> special case has a lower possible  $C_V$  value for maintaining critical damping. A smaller  $C_V$  value is generally desirable, because it minimizes the power required by the virtual capacitor to mimic a real capacitor. This is because the power of the virtual capacitor,  $P_{C_V}$ , is linearly related to  $C_V$  as shown in Eq. (4.2). Minimizing the power required also minimizes the required energy utilized by the virtual capacitor during damping actuation. This minimizes the range of the PCM power negatively affecting the virtual stabilizer performance and minimizes ES energy usage. However, a higher  $R_V$  from the 2<sup>nd</sup> special case solution region can attenuate the  $\frac{dV_{MVDC}}{dt}$  term, using the low-pass filter, which can offset the effects of a higher  $C_V$  value. However, this entire discussion focuses



Figure 4.10: Low-Q Solution Space

purely on small signal stability. For large signal stability, generally, a higher  $C_V$  value is desirable to maximize the virtual capacitance to provide more buffer energy to stabilize a larger disturbance.

## 4.3.4 Dynamic Stabilizer Tuning

The large range of power throughput through the system causes the small signal stability region to drastically shift. One solution is to overly over-damp the system during low power throughput, so that the system will be only slightly over-damp or critically damp when the system operates near its max power ratings. However, overly over-damping the system can cause any voltage droop signaling to be slow during low power throughput, which may be undesirable depending on the final MVDC system reliance on voltage droop information. This thesis employs dynamic tuning of the virtual stabilizer, maintaining a target damping factor near critical damping for the entire power operating range of the system. This allows voltage levels to quickly converge to its voltage droop levels, minimizing voltage droop information transmission time.

To generate the virtual stabilizer's values for dynamic tuning, the solving methodology in Algorithm 2 was modified. The algorithm used for solving the dynamic tuning values is shown in Algorithm 3. The general idea is to sweep the range of the equivalent load resistance of the CPL to find the values for  $C_V$  and  $R_V$  that maintains a set target damping factor. First, the analytical damping factor formula for either low-Q approximation 1<sup>st</sup> or 2<sup>nd</sup> special case is simplified by plugging in R, L, and C, using the known system values. Setting the damping factor formula equal to the target damping factor, MATLAB then solves for  $R_V$ , setting one side to  $R_V$  and the other side a mix of values and the variables  $C_V$  and  $R_L$ , creating an equation in the form of  $R_V(C_V, R_L)$ .

### **Algorithm 3** Calculate $C_V$ Lookup Table for Dynamic Tuning of the Virtual Stabilizer

1: Initialize values for  $R, L, C, \zeta_{target}$ 2:  $R_V(C_V, R_L) \leftarrow \text{Solve}(\zeta_n(R, L, C, R_V, C_V, R_L) = \zeta_{target}, R_V)$ 3:  $C_V(R_L) \leftarrow$  Zero Array of dimension  $[R_L \text{ Range}]$ 4: for all  $R_L$  in  $R_L$  Range do  $C_V \leftarrow 0$ 5:while True do 6:  $C_V \leftarrow C_V + StepSize$ 7:  $R_V \leftarrow \text{Numerically Solve}(R_V(C_V, R_L))$ 8:  $a_3, a_2, a_1, a_0 \leftarrow \text{Calculate Transfer Function}(R, L, C, R_L, C_V, R_V)$ 9:  $\hat{a_3}, \hat{a_2}, \hat{a_1} \leftarrow \text{Normalize}(a_3, a_2, a_1, a_0)$ 10:Calculate Case $(\hat{a}_3, \hat{a}_2, \hat{a}_1)$ 11:if Special Case n then 12: $\zeta \leftarrow$  Special Case n Damping Factor 13:else 14: $\zeta \leftarrow 0$ 15:if  $\zeta = \zeta_{target}$  then 16: $C_V(R_L)[R_L] \leftarrow C_V$ 17:Break 18:19: Return Lookup Table  $C_V(R_L)$ 

#### 4.3. Low-Q Approximation

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A sweep searching for a  $C_V$  value is done for each  $R_L$  value, and the  $C_V$  value must result in the targeted damping factor. By plugging  $R_V(C_V, R_L)$  into the transfer function and running low-Q approximation, the  $R_V$  term is therefore replaced by a value dependent on the searched  $C_V$  and  $R_L$  terms. Then, the solver low-Q approximates for the target damping factor for the chosen special case, finding a set  $C_V$  value to pair with the numerically solvable  $R_V$  value. This results in  $C_V$  being dependent on only  $R_L$  in the form of  $C_V(R_L)$ . Therefore, the previous variable dependence of  $R_V(C_V, R_L)$  becomes  $R_V(C_V(R_L), R_L)$ , translating into  $R_V(R_L)$ . This means that both  $C_V$  and  $R_L$  values would purely be dependent on the  $R_L$ term. The  $C_V$  values that result in the target damping factor for the range of  $R_L$  are stored in a lookup table for usage, and linear interpolation was used to fill in the gaps between each step points. A lookup table was used because finding  $C_V$  using this method is time consuming and should be precomputed off-line.  $R_V$  can be calculated on-line as the analytic equation  $R_V(C_V, R_L)$  is solved by simply plugging in the dependent terms.



# Chapter 5

# **Theory Verification**

Validation was done using MATLAB Simulink simulations to confirm that the MVDC stabilizer theory is correct. First, the equivalent circuit of the MVDC PCM with virtual stabilizer was validated against the "real" PCM model with virtual stabilizer control. Next, the transfer function was validated to be equivalent to the equivalent circuit. Finally, the low-Q approximation method of tuning the virtual stabilizer was validated along with dynamic tuning.

First, realistic values must be chosen. However, because the physical properties of the MVDC are not set in stone, realistic values may only be approximated. The MVDC system simulation values are shown in Table 5.1. Using [24], it is assumed that the PCM employs 10kHz DC/DC power converters. Using [19] and [11] as references, the RLC values were chosen. For this model, the R term was reduced as the load power is greater in this model, causing a much more drastic voltage sag. This is because a higher power load will have a smaller equivalent load resistance, causing the equivalent voltage divider to sag the voltage more. Also, instead of directly using the MVDC bus capacitance from the referenced papers, an extra bus capacitor of 1mF was added for minimal large signal stability. This bus capacitance is not large enough to provide small signal stability across the full load operating range for the simulated CPLs.

The PCM has many control loop and hardware values that must be chose. The chosen PCM values are shown in Table 5.2. [25] was used as a reference to approximate most of the PCM

#### 5.1. Small Signal Stability Criteria

Variable	Value
R	$0.1\Omega$
L	2.0mH
C	$1.03 \mathrm{mF}$
Nominal $V_{MVDC}$	12kV
$V_{NL}$	$12.6 \mathrm{kV}$
$V_{FL}$	11.64kV
I <sub>PGMMax</sub>	10kA
$\frac{d}{dt}i_{PGM}$ Limit	$\pm 100A$

Table 5.1	: MVDC	System	Values
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values.

Table 5.2: PCM System Values

Variable	Value
$K_P$	2
K <sub>I</sub>	5
$K_R$	0.00001
$C_{IBUS}$	$0.01\mathrm{F}$
$V_{IBUS}^*$	$6 \mathrm{kV}$
$E_{ES}^*$	1.056 GJ
$E_{ESMax}$	$1.32 \mathrm{GJ}$
$i_{PCM}$ Limit	0 to $10$ kA
$\frac{d}{dt}i_{PCM}$ Limit	-3 to $3$ kA/s
$i_{ES}$ Limit	-1.76 to 1.76kA
$\frac{d}{dt}i_{ES}$ Limit	-3.333 to $3.333$ kA/s
$\frac{d}{dt}i'_{PGM}$ Limit	-200 to 200A
Tol	10 V

# 5.1 Small Signal Stability Criteria

Using the small signal stability criteria Eq. (4.1), at 12kVDC nominal bus voltage, the circuit is considered small signal stable to the maximum CPL power of 7.416MW. To prove this, a CPL is set to an initial constant power consumption of 1MW, and the CPL is ramped up to



21MW at a 400kW/s ramp rate. The RLC values in Table 5.1 were used.

Figure 5.1: Simplified MVDC model used for testing.

In the simulations, there are oscillations at the beginning caused by startup settling, but the bus voltage quickly converges to a nominal voltage. A 5 second hold time was provided before the CPL ramps its power consumption for startup settling.

Upon loss of stability, both the PCM and equivalent resistive CPL cause unacceptable bus voltage oscillations, and the equivalent resistive CPL experiences a bus voltage collapse due

#### 5.1. Small Signal Stability Criteria

to the loss of voltage stability. The PCM does not allow the bus voltage to collapse to a steady zero, because the internal controller oscillates between its current limits, causing the bus voltage oscillation to continue. From Fig. 5.1b, both CPLs lose voltage stability above 18MW load power during power ramping. The PCM loses stability at a lower power consumption than the equivalent resistor CPL. Nevertheless, both loads remain small signal stable at a higher power level than the small signal criteria suggests. The bus voltage does start above nominal voltage and droop down as intended, but this elevated bus voltage would not cause a doubling of the small signal stable power ceiling. This shows that the criteria underestimates when the system loses small signal stability for the chosen ramp rate. The definition of a large and small signal perturbation is loose, so the chosen power ramp may be a smaller small signal perturbation than expected.

The virtual stabilizer, if we ignore the  $R_V$  term, will increase the overall bus capacitance and dampen the system at with a higher load power. Relating it back to Eq. (4.1), it would increase the *C* term, increasing the small signal stability power ceiling. This is because  $C_V$ is effectively a parallel capacitor to *C*. Realistically, the RC stabilizer allows a smaller added  $C_V$  term for stabilization, which is preferred as a higher  $C_V$  results in more power used by the virtual stabilizer as seen in Eq. (4.2).

To verify that the virtual capacitor can increase the small signal stability threshold, the power ramp simulation was repeated with an RC stabilizer using the values in Table 5.3. The PCM CPL used a virtual stabilizer and the equivalent resistor CPL used real RC components. The new small signal stable power ceiling should be 14.616MW. The results are shown in Fig. 5.2. Note that these values were not chosen to critically, over, or under damp the system but to only increase the power ceiling for the stability criteria of Eq. (4.1).

The results show that the loads are stable for the entire 20MW ramp and that the added stabilizer increased the small signal stable power ceiling. As noted before, Eq. (4.1) under-



Table 5.3: Tested Virtual Damper Values

Value

Variable

Figure 5.2: Compared Circuits for Step Response.

estimates for this scenario, so it was expected that both loads remained small signal stable for the whole power ramp despite the 14.616MW power ceiling for stability.

The virtual and real RC stabilizer capacitor power were measured and shown in Fig. 5.3. It is visible that in both real and virtual implementations, the capacitor is discharging the same amount of power. The real capacitor's power only rings when the voltage starts and stops drooping, which is expected. Unexpectedly, the virtual capacitor's power rings during the continuous discharge outside the start and stop of the voltage droop. This shows that the virtual and real capacitors behave in a similar but not equal manner.

The hardware-limited and raw virtual stabilizer capacitor current  $I_{C_V}$  were measured. One of the oscillation points was zoomed in and shown in Fig. 5.4. The resulting graph appears blocky as the simulation uses a maximum timestep of 10  $\mu$ s with zoomed 0.7 ms time range. Since the PCM power converter is assumed to be switching at 10kHz, the simulation time

#### 5.1. Small Signal Stability Criteria



Figure 5.3: Compared Real and Virtual RC Stabilizer Power.

step is 10 times finer than what a real converter can output, so the noticeable simulation stepping can be ignored. The results show that the hardware limitations are barely causing a change in the actual  $I_{C_V}$  from the raw  $I_{C_V}$ . Also, note that the virtual stabilizer's RC time constant frequency is 16kHz, which is not realistically feasible for a 10kHz converter to accurately emulate, but this simulation is only for behavioral verification purposes. A critically or over damp-system will not have such a tiny RC stabilizer time constant.

The virtual RC stabilizer current was compared with the PCM's ES current to confirm that the ES canceled out the virtual stabilizer's fluctuations on the PCM's internal DC bus. The results are shown in Fig. 5.5. The ES does have a negative current compensating for the stabilizer's fluctuations. The other components of the ES's current waveform are for maintaining the internal DC bus voltage and later on recharging the ES.



Figure 5.4: Compared Raw and Hardware Limited Virtual Stabilizer Currents.



Figure 5.5: PCM ES Cancels the Virtual Stabilizer's Fluctuations.

#### 5.2. Equivalent Circuit Validation

## 5.2 Equivalent Circuit Validation

As the previous results show, the PCM and equivalent resistor CPL do not exactly agree in behavior. The equivalent circuit of a CPL with the stabilizer must closely model the PCM and virtual stabilizer system. This is to ensure that the equivalent circuit can actually be used for analysis. However, as the virtual stabilizer was modeled to behave similarly to a RC arm parallel to the load, it should be expected that both real and virtual parallel RC dampeners are still similar in behavior. The PCM has extra limitations and features over the equivalent resistance CPL that causes the behavior to diverge. This divergence should be in the PCM's favor as the PCM will inhibit unstable effects from large signals.

To compare the behaviors of the PCM and real resistor CPL along with virtual and real RC dampers, step responses of each system were simulated. The RLC values from Table 5.1 are used as done before. The virtual and real stabilizers are still using the values from Table 5.3. These values are known to under-damp the system by low-Q approximation, which will shown later in Section 5.4. An under-damp system was chosen to make oscillations visible to detect any phase shifts in the step responses

Recall that the PCM has a virtual limit on the load power ramp transmitted to the MVDC bus to mimic the MVDC generator's ramp rate limitation. The virtual ramp rate limit is 1.2MW/s before the ES in the PCM will provide large signal stability compensation. The equivalent R load will not exhibit this behavior as it does not have internal ES. Therefore, the CPL step signal must not trigger the PCM's ES when comparing the systems. The load power step used in this test is from 1.000MW to 1.0012MW in 1ms, providing a ramp rate of 1.2MW/s. This way, the power consumption from the MVDC bus by the two load systems should be close to equal.

Shown in Fig. 5.6, these separate circuits were simulated simultaneously: equivalent R with

real RC stabilizer, PCM with real RC stabilizer, and PCM with virtual RC stabilizer. The results of this simulation is shown in Fig. 5.7.



Figure 5.6: Compared Circuits for Step Response.



Figure 5.7: Step Responses to 1.2kW 1ms Step.

There is a no noticeable phase shift and mostly a magnitude error between all of the responses. The PCM and equivalent resistance CPLs appear to have equal step responses

#### 5.2. Equivalent Circuit Validation

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when both use a real RC stabilizer, but the virtual and real RC stabilizers have a more noticeable magnitude error when using a PCM CPL. This magnitude error gives the virtual RC stabilizer a greater advantage as the bus voltage settles quicker, and the oscillation itself has a lower magnitude. Direct voltage magnitude error comparisons were made in Fig. 5.8. The small millivolt errors between each system should be negligible. To further emphasize how tiny the errors are: the V/W ratio of the peak errors for a 1.2kW step is approximately  $6.7 \frac{\mu V}{W}$  for Fig. 5.8a and  $12.5 \frac{\mu V}{W}$  for Fig. 5.8b. The errors scaled to a 1MW step would be 6.7V for Fig. 5.8a and 12.5V for Fig. 5.8b, which is less than 0.2% of the nominal bus voltage. However, a 1MW at 1ms would result in a 100MW/s ramp rate, which is unrealistic for the generator to support.

The magnitude errors exists because the virtual RC stabilizer is minutely affected by the physical limitations on the PCM's power and ramp rates. The magnitude error can be considered an advantage to the virtual RC stabilizer as the oscillations would have lower magnitude. With no phase shift and very tiny magnitude errors, all 3 models are fairly equivalent, and should introduce little errors in using the equivalent circuit for further analysis.





(a) Bus Voltage Error Between a Real RC Stabilizer with a PCM CPL and Equivalent R CPL



(b) Bus Voltage Error Between a PCM with Real RC and Virtual RC Stabilizer
Figure 5.8: Bus Voltage Errors Between Ideal Equivalent Circuit and Simulated PCM

#### 5.3. Transfer Function Validation

## 5.3 Transfer Function Validation

MATLAB Simulink supports a transfer function block which allows the user to plug in the full transfer function to calculate the transfer function's response to an input. The equivalent circuit and the transfer function had the same input and ran in parallel in the same Simulink simulation. A unit step input signal was used in this simulation. The simulation parameters are the same as done in Section 5.1. The CPL and its equivalent resistive value were calculated to behave as a 10MW CPL at 12kVDC. The results of this simulation is shown in Fig. 5.9. The equivalent real circuit and the transfer function have exactly the same step response.



Figure 5.9: Equivalent circuit and transfer function validation simulation results.

From the results, the passive component equivalent transfer function is considered equivalent to the PCM model. Low-Q analysis can now be used on the equivalent transfer function to calculate the virtual RC stabilizer values to critically or over damp the PCM model to remove the oscillations.

# 5.4 Low-Q Approximation Validation

The methodology for validating the low-Q validation is done in a series of steps. First, RLC and the equivalent load resistance of the CPL are statically assigned values. Next, the circuit transfer function is low-Q approximated with a set of  $C_V$  and  $R_L$  values as done in Algorithm 2, finding the system damping factors for these values. A  $\alpha$  value of 0.05 was used for low-Q approximation. Then, the step response of the virtually damped system is plotted. The step response should reflect a behavior matching the approximated damping factor.

Using the previous step response values, a 10.0MW load at 12kVDC will have an equivalent negative resistance of 14.4 $\Omega$ . RLC values from Table 5.1 were used as in all other previous simulations. The virtual stabilizer values of Table 5.3 are marked on the graph in Fig. 5.10, resulting in an approximate damping factor of 0.01621. This makes the system very underdamp, which matches the behavior of the oscillations in the step response of Fig. 5.9.

In the low-Q approximation graph of Fig. 5.10, there are two special case regions as mentioned in Section 4.3.4. The 1<sup>st</sup> special case is the lower  $R_V$  region, and the 2<sup>nd</sup> special case is the upper  $R_V$  region. Both solutions approach a peak damping factor saddle shape before hitting the forbidden region. While the 1<sup>st</sup> special case region has a smaller  $C_V$  value, the 2<sup>nd</sup> special case region solution is preferred, because the 2<sup>nd</sup> special case region results in a higher frequency stabilizer. This will be shown later in this section. The black lines in the plot represents the critical damping line, where the stabilizer achieves critical damping of the system. Critical damping is desirable, because the MVDC voltage response is quick with no oscillations.

To show how the damping factor changes as the CPL equivalent negative resistance changes, two simulations were executed. The first simulation uses a  $144\Omega$  equivalent negative resistor

#### 5.4. Low-Q Approximation Validation



Figure 5.10: Low-Q Approximated Damping Factors for 10MW CPL  $(R_L=14.4\Omega)$ 

for a CPL of 1MW at 12kVDC CPL, and the results are shown in Fig. 5.11a. The second simulation uses a  $1.44\Omega$  equivalent negative resistor for a CPL of 100MW at 12kVDC CPL, and the results are shown in Fig. 5.11b.

We can see that the critical damping lines squeeze into the overdamping saddle as the CPL's equivalent negative resistance shrinks. This shows that: to prevent oscillations, one must either over-damp when the CPL is at low power consumption or dynamically tune the virtual stabilizer to maintain a quick critical damping. Also, a negative damping factor appears at 100MW CPL, showing that certain virtual damping values causes the MVDC bus voltage to diverge.

Values for the virtual stabilizer were picked from Fig. 5.11b. The chosen points are shown in Fig. 5.12 and listed in Table 5.4. One set of values were picked from the  $1^{st}$  special case solution and another set were picked from the  $2^{nd}$  special case.



Figure 5.11: Low-Q Approximated Damping Factors from Virtual Damper Values Sweep

#### 5.4. Low-Q Approximation Validation



Figure 5.12: Selected Test Points for 100MW CPL  $(R_L = 1.44\Omega)$ 

The step response of each of the chosen points in Table 5.4 are shown in Fig. 5.13 and Fig. 5.14. The step responses were generated using the actual transfer function, exhibiting the actual system behavior rather than approximating it. The under-damp systems do exhibit overshoot or slight oscillation. The critically damp systems do not overshoot drastically or oscillate. The overdamp systems generally have slower rise times. The unit step responses do not converge towards 1 due to the resistive terms from the MVDC bus forming a voltage divider. The divider causes a voltage rise rather than a voltage drop due to the CPL's

$C_V$ (F)	$R_V(\Omega)$	$\zeta$	Special Case
0.0294	0.2522	0.6189	1
0.0714	0.233	0.9952	1
0.1202	0.1582	0.998	1
0.1198	0.231	1.316	1
0.0656	0.605	0.6999	2
0.1002	0.4708	0.9914	2
0.15	0.4658	0.9968	2
0.15	0.3862	1.267	2

Table 5.4: Picked Virtual Damper Values from Fig. 5.12

negative resistance.

It is visible that the 2<sup>nd</sup> special case stabilizers do have a significantly faster initial response to approach over 80% of equilibrium. However, the response quickly slows down, taking longer to completely converge to equilibrium than the 1<sup>st</sup> special case stabilizers. The faster initial response is caused by the system being designed to fall under the 2<sup>nd</sup> special case of low-Q approximation, causing a smaller time constant root term to be dominant in the system. However, to fall under the 2<sup>nd</sup> special case's solution space, the virtual stabilizer has a larger time constant (lower frequency), causing the slower final approach to equilibrium. Finally, all of these virtual stabilizers have small enough RC time constants to be very realistic for 10kHz power converters to emulate.

It is up to the system designer to determine which special case stabilizers perform better. The 2<sup>nd</sup> special case solution does move near equilibrium faster, but does take longer to settle towards equilibrium. The 1<sup>st</sup> special case solution moves near equilibrium at a more steady speed, and settles at equilibrium faster than the 2<sup>nd</sup> special case solutions. Never the less, the results do show that the low-Q approximation does give a good approximation on the system's damping factor and that low-Q approximation can be used to determine the desired values of the virtual stabilizer.

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### 5.4. Low-Q Approximation Validation







Figure 5.14: 2<sup>nd</sup> Special Case Step Responses  $(R_L = 1.44\Omega)$ 

#### 5.5. Dynamic Tuning Validation

## 5.5 Dynamic Tuning Validation

A shown in Section 4.3.4, the virtual stabilizer can be dynamically tuned. A lookup table can be generated to store each  $C_V$  value for each  $R_L$  operating point, and  $R_V$  would be calculated from the previous two values. To validate the dynamic tuning method, a set of  $C_V$  and  $R_V$  values were calculated to a corresponding  $R_L$  value, and the virtual stabilizer values should match the brute forces values in Fig. 5.15. In this validation process, the system values from Table 5.1 were used with a target damping factor of 1.1 and only using the 1<sup>st</sup> low-Q approximation special case with a  $\alpha$  of 0.05. A target damping factor of 1.1 was chosen. Slight over-damping was chosen instead of critical damping to ensure the system is never slightly under-damp due to low-Q approximation error.

To solve  $R_V(C_V, R_L)$  for Algorithm 3, Eq. (4.18) was set equal to the target damping factor of 1.1. Eq. (4.24) would be used if the 2<sup>nd</sup> special case solution region was used instead. Using MATLAB's solve operator to solve for  $R_V$ , the resulting analytic equation for  $R_V$  is

$$R_V(C_V, R_L) = \frac{71L - 71CRR_L + 50C_VRR_L \pm 11A}{50(C_VR - C_VR_L)},$$

$$A = \sqrt{21C^2R^2R_L^2 - 142CLRR_L + 100CLR_L^2 - 100C_VCR^2R_L^2 + 21L^2 + 100C_VLR_L^2}.$$
(5.1)

Note that there is a plus-minus square root in Eq. (5.1), and one must plug in a set of valid real values to find whether the square root term must be added or subtracted to result in a valid positive solution. The RLC values were plugged into Eq. (5.1), and the  $C_V(R_L)$  look up table was solved using Algorithm 3. The resulting tuning values for the virtual stabilizer are shown in Fig. 5.16. Comparison between the low-Q approximation brute forced expected values and the actual analytically solved low-Q approximation values are shown in Table 5.5.





Figure 5.15: Expected Dynamic Tuning Result Points

#### 5.5. Dynamic Tuning Validation

Overall, the calculated values of the virtual stabilizer have little error from the brute forced values for maintaining a 1.1 damping factor. This validates that the methodology for solving the dynamic tuning values using is accurate and correct.



Figure 5.16: Virtual Stabilizer Dynamic Tuning Values for  $\zeta = 1.1$ 

Table 5.5: Brute Forced and Analytically Solved Virtual Stabilizer Dynamic Tuning Values

	Brute Forced		Solved		
$R_L(\Omega)$	Damping Factor $(\zeta)$	$R_V(\Omega)$	$C_V$ (F)	$R_V(\Omega)$	$C_V$ (F)
144	1.096	0.2732	0.0704	0.2733	0.0709
14.4	1.098	0.2694	0.0718	0.2695	0.0720
1.44	1.100	0.2360	0.0838	0.2362	0.0837

# Chapter 6

# Results

With the modeling and approximation theory verified, the virtually stabilized PCM can be simulated with a pulsed load. MATLAB and Simulink were used for generating these results. The same system parameters in Table 5.1 Table 5.2 were used. The CPL will have a baseline 2MW constant power load, and a pulse load applying a pulse train with 258MJ of energy per pulse at 4 pulses per minute. The pulse train will have 5 pulses, and each pulse is 10 seconds long with a 5 second baseline power load period between each pulse. The pulse will ramp up and down at 10.75MW/s for 4 seconds both ways, holding its peak load of 43MW for 2 seconds per pulse. The pulse train begins after a 5 second idle time for the simulator to settle any simulation start up fluctuations.

A system without the virtual stabilizer was first used to show that the system is not small signal stable as the PCM's load power on the MVDC bus goes up. The results are shown in Fig. 6.1. The MVDC bus voltage droops up and down with the pulse, but the overall bus voltage droops more after each pulse due to the ES ramping up its recharge power. This causes the PCM to progressively draw more power from the MVDC bus after each pulse. The MVDC bus voltage does begin to oscillate during the 3<sup>rd</sup> pulse, but the bus voltage recovers as the PCM's load power on the MVDC bus decreases. However, the MVDC bus voltage oscillates and loses control during the 4th pulse.

To show what the proper behavior of the system should be, the virtual stabilizer was added using statically assigned values from Table 5.5.  $C_V = 0.0837$  and  $R_V = 0.2362$  for a 1.1


Figure 6.1: Pulse Train Without Stabilizer - Bus Voltages

damping factor when a 100MW is loaded on the MVDC bus was used. The bus voltages with the virtual stabilizer is shown in Fig. 6.2, and the currents of the PCM components at  $V_{IBUS}$  is shown in Fig. 6.3. The MVDC bus voltage never oscillates during the pulse train, showing it is small signal stable. The PCM ES SoC and actual energy is shown in Fig. 6.4. This shows ES compensating the large power swings of the pulsed load and recharging after the pulse train.



Figure 6.2: Pulse Train With Statically Tuned Virtual Stabilizer - Bus Voltages

The power of the hardware-limited virtual stabilizer is shown in Fig. 6.5. Virtual stabilizer

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#### Chapter 6. Results



Figure 6.3: Pulse Train With Statically Tuned Virtual Stabilizer - PCM Currents



Figure 6.4: Pulse Train With Statically Tuned Virtual Stabilizer - ES Energy

is reducing or increasing the PCM's load power by kilowatts of power to provide small signal stability, and the stabilizing signal has a consistent shape per pulse in the pulse train. There is a slight but noticeable increase in the magnitude scaling of the power responses in the later pulses. This is because the CPL's power load on the MVDC bus is higher and more



destabilizing, and the stabilizer needs to scale the stabilizing response up to compensate.

Figure 6.5: Statically Tuned Virtual Stabilizer Power

Next, the same pulse train simulation and system parameters were simulated with the virtual stabilizer using dynamic tuning values found in Section 5.5 for a 1.1 damping factor. The bus voltages are shown in Fig. 6.6, and the MVDC bus voltage is still stable. The internal PCM currents are shown in Fig. 6.7, which appears similar to the statically tuned virtual stabilizer. The energy of the ES, shown in Fig. 6.8 is also similar.

The power of the dynamically tuned virtual stabilizer is shown in Fig. 6.9. The stabilizer is much more noisy than the statically tuned one. However, the dynamically tuned stabilizer does use marginally less power than the statically tuned one. The measured  $R_L$  and dynamically tuned  $C_V$  and  $R_V$  values are shown in Fig. 6.10.

Chapter 6. Results



Figure 6.6: Pulse Train With Dynamically Tuned Virtual Stabilizer - Bus Voltages



Figure 6.7: Pulse Train With Dynamically Tuned Virtual Stabilizer - PCM Currents



Figure 6.8: Pulse Train With Dynamically Tuned Virtual Stabilizer - ES Energy



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Chapter 6. Results



Figure 6.10: Dynamically Tuned Virtual Stabilizer Values

## Chapter 7

## **Discussion and Future Work**

From the validation work, the virtual and real RC small signal stabilizers do not exhibit exactly the same behavior. However, the negative load virtual stabilizer still provides small signal stabilization. From the results, the virtual stabilizer can provide MVDC bus small signal stabilization while a pulsed CPL is running a pulsed train. The modified control loops in this thesis performed well despite the fact that the original control loops were not developed or tested for pulsed power loads [6, 17]. The modified control loops provided the needed pulsed power in a stable manner while maintaining the ES adequately and following hardware ramp rate limitations.

The virtual stabilizer does not introduce enough power fluctuations to greatly impact the power quality to the downstream load compared to the overall CPL's power consumption. Also, the power is low enough that the stabilizer can simply run with statically tuned values. The dynamically tuned stabilizer does have a smaller power fluctuation compared to the statically tuned stabilizer, but it is a very small difference compared to the CPL's power consumption. Also, the  $R_L$  feedback causes noise on the dynamically tuned stabilizer's power fluctuations.

When zoomed in, there are very tiny oscillations on the  $R_L$  signal, because the MVDC bus voltage is has tiny noise caused by the MVDC system dynamics, causing the  $R_L$  signal to oscillate. However, with the MVDC bus voltage noise feeding into the dynamic tuning loop of the virtual stabilizer, the output stabilizer values also contains this noise, causing the



#### Chapter 7. Discussion and Future Work

stabilizer power fluctuations to also have the noise. This noise is added into the PCM power consumption from the MVDC bus, which causes further MVDC bus voltage noise. The system is damp enough where this small signal noise does not cause the MVDC bus voltage to fluctuate out of control, and the ES does adequately cancel the fluctuation noise on the internal DC bus. However, the noise on the virtual stabilizer power is undesirable as it lowers power quality and puts more stress on the MVDC bus facing power converter in the PCM.

Compared to a real RC stabilizer, the virtual stabilizer does eliminate power losses across the resistor when the capacitor charges or discharges. Also, since the whole virtual stabilizer system uses existing components, there is ample space and weight saving. A capacitance of 83.7mF, used in the statically tuned stabilizer, rated for 12kV usage would at least store 6MJ of energy. However, the capacitor would normally be rated for a much higher voltage for safety reasons. From [3], a 6MJ capacitor will have an estimated volume of 6  $m^2$  and mass of 7380kg. The resistor will also take up space and tonnage. Also, the components may need some cooling and wiring hardware, consuming even more tonnage and space.

In the future, the dynamic tuning control loop could be improved to filter out the retuning noise. Also, the reduced MVDC system could be expanded with a parallel PCM or employ realistic generators and switching power converters. With a parallel load, the MVDC system has an increased complexity and a higher order transfer function. It should be investigated how well low-Q approximation enables system designers to calculate system damping factors for a scaled complexity. Finally, the control loop proportional and integrator loops could be refined or mathematically modeled for improved tuning. The MATLAB Simulink code used in these simulations are available in Appendix A.

## Chapter 8

### Conclusions

A controls system was successfully implemented for a pulsed power load prototype. This controls system handles auxiliary pulsed load hardware, PFN charging and discharging, and data acquisition. Due to the optimization work done, it is capable of operating the PFN to generate very precise pulse waveforms for experimental purposes.

Then, a PCM control system supporting a virtual negative load small signal stabilizer was developed for a MVDC system with a large pulsed load. The PCM control loops manage the PCM's internal DC bus voltage and ES adequately for pulsed loads. The ES is recharged after buffering the large power swings of the pulsed load within an acceptable amount of time. The virtual stabilizer has been proven to increase the small signal stable power range of a reduced MVDC system. A methodology was developed in tuning the virtual stabilizer, and the control loop uses the ES to cancel the stabilizer's power fluctuations. The stabilizer can also be on-line dynamically tuned, minimizing the stabilizer's power signal.

Dynamic tuning of the negative load virtual stabilizer did not perform as well as expected as it introduced more noise than a statically tuned stabilizer. However, the dynamically tuned stabilizer does have a reduced magnitude in its power fluctuations as expected. Overall, the power fluctuations of the virtual stabilizer is small enough that dynamic tuning may not be required. As predicted, both virtual stabilizers did increase the small signal stability range of the system using existing components rather than adding additional real hardware.

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# Appendices

## Appendix A

## MATLAB Simulink Code Blocks

The Simulink code blocks used in this paper are shown here. These are the same Simulink code blocks used to generate the results in Chapter 6. Some modifications were done to the shown Simulink code blocks to generate the validation results in Chapter 5, but they have the same control logic and variable values as stated in the respective chapters.

The MVDC bus Simulink code block is shown in Fig. A.1. This holds the PCM block and the simplified MVDC bus circuit. There is some minor logic for the voltage droop, and there are some data output blocks for viewing simulation results.

The full PCM Simulink code block is shown in Fig. A.2 and Fig. A.3. This control block implements the proposed PCM control loops in Chapter 4. The PCM circuit is also implemented in the blue code blocks. Finally, there are various data acquisition points for measuring values at various nodes.

For dynamic tuning, the PCM Simulink code blocks for the virtual RC stabilizer is modified with the code block shown in Fig. A.4. The Simulink transfer function block was replaced with an equivalent implementation, because it does not support dynamically changing transfer function values. The "Lookup-VC(RL)" lookup table block is for finding  $V_C(R_V)$ , and  $V_R(R_L)$  is found with the function block "VR(RL)." The final output is the power of the virtual capacitor behind the virtual resistor. Appendix A. MATLAB Simulink Code Blocks



Figure A.1: MVDC Bus Simulink Code Blocks



Figure A.2: Full PCM Simulink Code Blocks - Part A

urr\_es\_E

PCM\_ES\_EMax

0.5\*PCM\_ES\_C

%SoC

sim\_EES

im SoCES

PCM\_IBus\_VNom

٠



81

VIBUS

LP-VIBUS

Appendix A. MATLAB Simulink Code Blocks



Figure A.3: Full PCM Simulink Code Blocks - Part B





Figure A.4: Dynamically Tunable Virtual RC Stabilizer Simulink Code Blocks